

Label-free composition determination for biomolecular condensates with an arbitrarily large number of components

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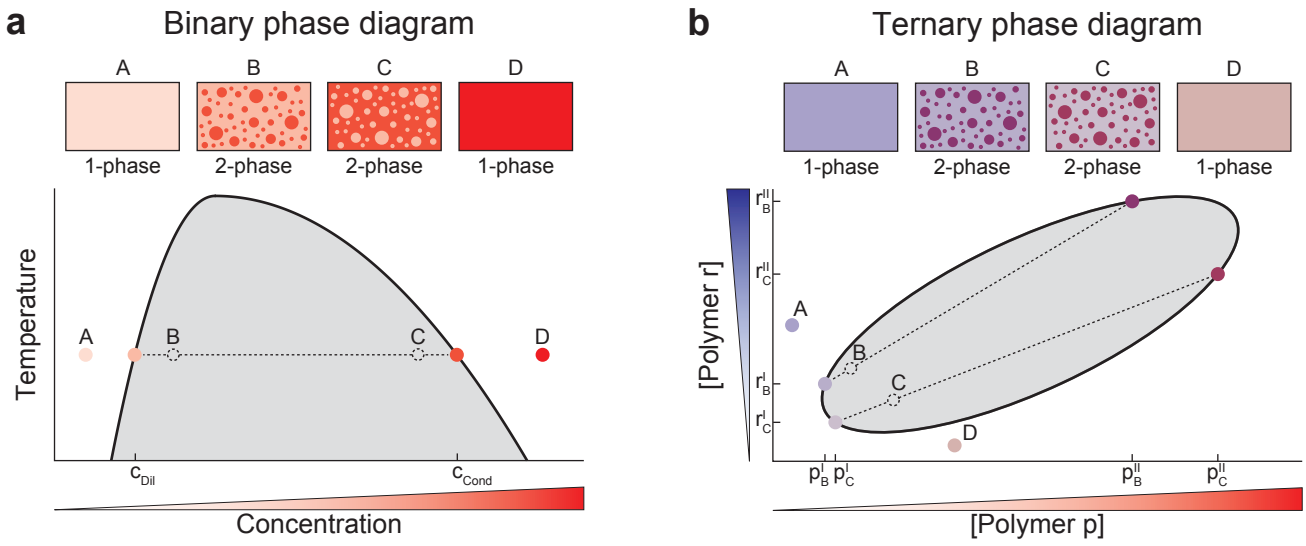
ABSTRACT (150 words)

Biomolecular condensates are membrane-less organelles made of multiple components, often including several distinct proteins and nucleic acids. However, current tools to measure condensate composition are limited and cannot capture this complexity quantitatively, as they either require fluorescent labels, which we show can perturb composition, or can distinguish only 1-2 components. Here, we describe a label-free method based on quantitative phase microscopy to measure the composition of condensates with an arbitrarily large number of components. We first validate the method empirically in binary mixtures, revealing sequence-encoded density variation and complex aging dynamics for condensates composed of full-length proteins. In simplified multi-component protein/RNA condensates, we uncover a regime of constant condensate density and a large range of protein:RNA stoichiometry when varying average composition. The unexpected decoupling of density and composition highlights the need to determine molecular stoichiometry in multi-component condensates. We foresee this approach enabling the study of compositional regulation of condensate properties and function.

INTRODUCTION

Many compartments in living cells exist as condensed phases of biopolymers, termed biomolecular condensates, which are demixed from the surrounding cytoplasm or nucleoplasm^{1,2}, and are implicated in a wide range of cellular processes³. Phase separation of a simple binary mixture of a polymer in solvent results in a dilute phase coexisting with a polymer-rich condensed phase (**Fig. 1a**). Although demixing of a single full-length protein in a binary mixture is often sufficient to reconstitute simplified condensates⁴⁻⁷, condensates *in vivo* contain dozens of components⁸⁻¹⁰. Indeed, the functional identity of a particular condensate

Fig. 1: Phase diagrams of binary and ternary mixtures



40 **Fig 1: Phase diagrams of binary and ternary mixtures**

41 **a**, Phase diagram in a prototypical binary mixture with sketches of samples prepared in the 1-
42 phase (A,D) and 2-phase regimes (B,C). Compositions of coexisting phases, c_{Dil} and c_{Cond} , lie
43 on the binodal curve (solid black) that separates the 1-phase (mixed) and 2-phase (demixed)
44 regimes. A tie-line (dashed black) connects compositions of coexisting phases to the
45 corresponding average composition (open dashed black circle). Varying average solute
46 concentration in the 2-phase regime (gray) changes the relative volumes of coexisting phases
47 but not their composition. **b**, Phase diagram in a prototypical ternary mixture with sketches of
48 samples prepared at different average compositions. Unlike the binary case, ternary mixtures
49 prepared at different points in the two-phase regime may lie on different tie-lines, yielding
50 compositionally distinct pairs of coexisting phases.

51

52 inside a cell is determined by its composition. Unlike binary systems, such multi-component
53 condensates possess a continuum of compositions ¹¹, each connected to a coexisting dilute
54 phase via a tie-line in a phase diagram (**Fig. 1b**). Changes in component abundance can thus
55 shift the system to a new tie-line, altering condensate composition and physical properties ^{12,13}.
56 Despite its central role in physically defining condensates and specifying their properties, the
57 composition of multi-component condensates *in vivo*, and component stoichiometries in
58 reconstituted systems *in vitro*, are largely unknown.

59 In multi-component systems, condensate composition is typically estimated by fusing
60 each molecular species to a spectrally-distinct fluorescent tag ^{12,14,15}. Although powerful,
61 fluorescent tags contribute to interactions between species and with solvent, potentially shifting
62 the thermodynamic balance that specifies phase composition ¹⁶. Interactions with the
63 condensed phase can also drive strong deviations in fluorophore characteristics relative to
64 behavior calibrated in the dilute phase ^{17,18,15}, confounding quantification. Label-free
65 techniques avoid these issues entirely, but existing approaches require harsh treatments and are
66 effectively limited to binary systems for native-like molecules. For example, traditional bulk
67 approaches like ultra-violet (UV) absorption ^{20,21} and thermogravimetric analysis ²² require
68 condensate dissolution or destruction and impose sample requirements that are often
69 inaccessible with the modest yields obtained by recombinant expression and purification of
70 endogenous cellular condensate components (**Supplementary Note 1**). Though confocal
71 Raman spectroscopy enables measurements of intact condensates ^{18,19}, the experimental
72 requirements of high laser exposure or nanoparticles for surface-enhancements may alter
73 condensate dynamics, and a calibration sufficient to resolve multi-component composition has
74 yet to be demonstrated.

75 Reflecting these limitations, recent UV absorption measurements of the composition of
76 condensates reconstituted from recombinant proteins looked exclusively at binary systems with
77 intrinsically disordered protein regions (IDRs) rather than the full-length proteins ²³⁻²⁵. This is
78 in part because those fragments could be purified with sufficient yield from bacteria following
79 denaturation. That is not an option in many cases, however, as bacteria lack the machinery
80 needed to add post-translational modifications (PTMs) or assist folding of certain protein
81 domains, and denaturants may irreversibly alter protein conformational ensembles. Thus, it
82 remains unclear how the additional features of native-like proteins, including PTMs, native-
83 like conformational ensembles, and the additional domains present in full-length proteins, will
84 change the picture now emerging for condensates formed from IDRs alone. As functional roles
85 for PTMs and structured protein domains accumulate alongside molecular parts lists ⁸⁻¹⁰, there

86 is a pressing need for methods to reveal condensate composition in more faithful reconstitutions
87 that include multiple native-like components.

88 Here, we present a label-free method to precisely measure the composition of micron-
89 sized condensates reconstituted from an arbitrary number of components. Overall, this method
90 requires 1000-fold less material than bulk label-free alternatives, which enables dynamic and
91 temperature-dependent measurements of condensates formed from full-length native-like
92 components. We demonstrate that quantitative phase imaging (QPI) can be used to extract
93 refractive index differences between demixed phases, Δn , which we convert to condensed-
94 phase concentration for binary systems. By combining these Δn with tie-line measurements,
95 we then show that the concentrations of an arbitrary number of individual species can be
96 resolved quantitatively in multi-component condensates. We demonstrate this explicitly for a
97 model ternary system of full-length FUS protein and RNA, and reveal unexpected features in
98 the composition of these multi-component condensates. Additionally, we find that protein
99 concentrations vary from 87 to more than 470 mg/ml in condensates depending on sequence
100 and use of labels, and uncover a dramatic increase in density with age that may underly
101 previous reports of mechanical hardening²⁶. By resolving the chemical composition of multi-
102 component condensed phases *in situ* and in unprecedented detail, we anticipate that this label-
103 free method will enable mechanistic studies of complex composition regulation of
104 biomolecular condensate properties and function with multiple native components.

105

106

RESULTS

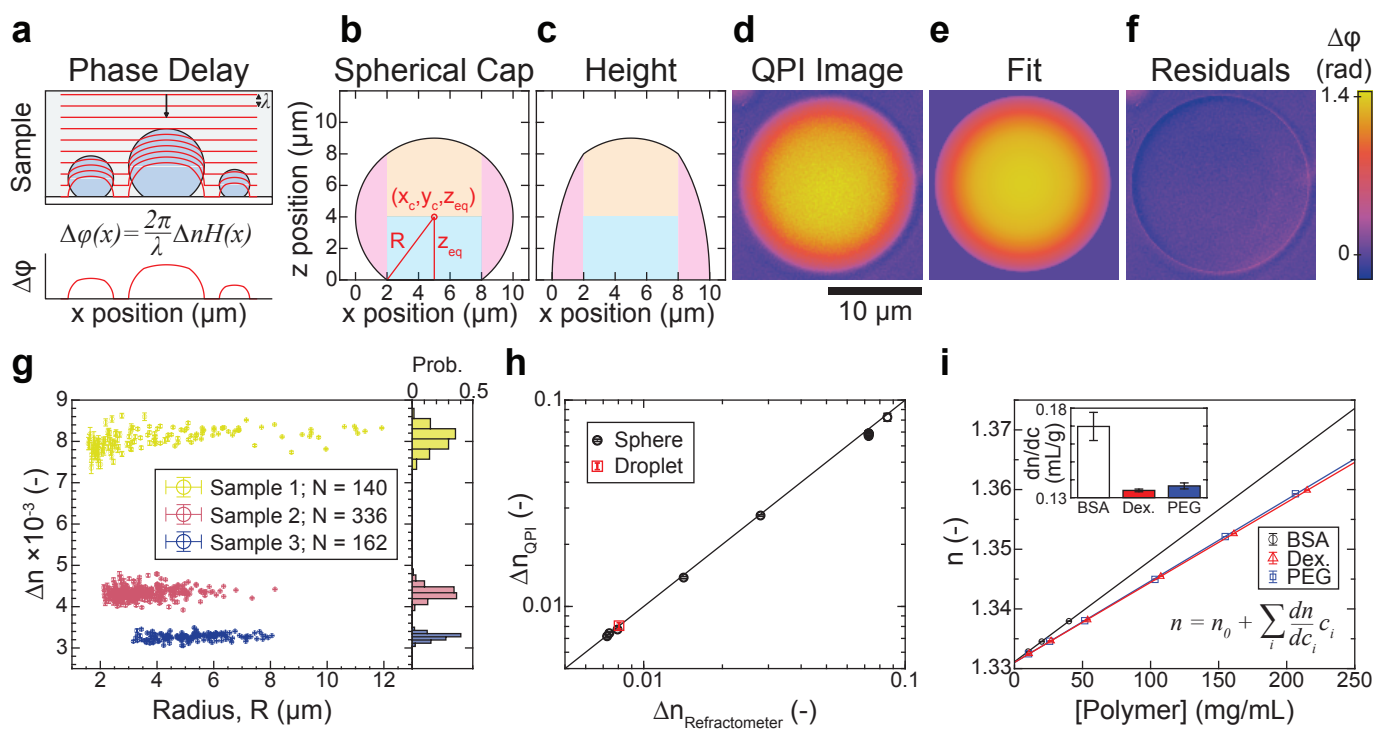
Optical concept

108 To measure the compositional difference between micron-sized droplets and the coexisting
109 dilute phase, we employ quantitative phase imaging (QPI)^{27,28}. Physically, QPI measures the
110 optical phase shift accumulated along a wavefront as it traverses spatial inhomogeneities in
111 refractive index within a sample, such as high-refractive index droplets immersed in a lower-
112 index medium (**Fig. 2a**). Within the first-order Born approximation²⁹, the optical phase shift
113 $\Delta\varphi$ measured by QPI at pixel (x, y) is proportional to the product of refractive index difference,
114 Δn , and droplet shape

$$115 \quad \Delta\varphi(x, y) = \frac{2\pi}{\lambda} \Delta n H(x, y), \quad (\text{Eq. 1})$$

116 where λ is the imaging wavelength and $H(x, y)$ is the projected height of the droplet along the
117 imaging axis. Thus, the refractive index difference between coexisting thermodynamic phases
118 can be obtained from the droplet's shape and optical phase shift. The refractive index of an

Fig. 2: QPI measures the refractive index of micron-size droplets *in situ*



120 **Fig 2: QPI measures the refractive index of micron-sized droplets *in situ***
121 **a**, Schematic of optical wavefronts (red) distorted by droplets on a flat surface (top) and the
122 cumulative optical phase shift (bottom). **b**, Schematic defining the geometry of a spherical cap.
123 **c**, Projected height profile $H(x)$ for the geometry in **b**. Shading in **b,c** denotes separate terms in
124 the analytic expression for $H(x)$, (see Methods). **d**, Phase image of dextran-rich droplet on
125 passivated glass. **e**, Fit of droplet in **d** to spherical cap. **f**, Residuals from fit. Scalebar in **e-f** is
126 10 μm . **g**, Refractive index difference Δn vs. droplet radius R extracted from fits to individual
127 dextran-rich droplets obtained from 3 different PEG/Dextran mixtures (colors). Error bars are
128 95 % confidence intervals. Probability histograms at right. **h**, Refractive index differences
129 measured with QPI vs. bulk refractometry for PEG/Dextran mixtures (red) or silica spheres in
130 different glycerol-water mixtures (black). Error bars are standard deviation. Solid line is $y = x$.
131 **i**, Refractive index is a linear function of component concentration for three model biopolymers
132 (BSA, Dextran, PEG). Inset: Slopes (dn/dc) for each polymer with 95 % confidence intervals.
133

134 aqueous protein solution is, in turn, a linear function of concentration over a wide range^{30,31}.
135 In this regime (see **Supplementary Note 2**), the condensed-phase protein concentration, c_{Cond} ,
136 in a binary system is given by

137
$$c_{Cond} = \frac{\Delta n}{dn/dc} + c_{Dil}, \quad (\text{Eq. 2})$$

138 where c_{Dil} is the dilute phase concentration and dn/dc is the slope of the concentration-
139 dependence of refractive index, which can be estimated from amino acid sequence³². This
140 suggests QPI is suitable to measure the concentration difference between a condensate and its
141 coexisting dilute phase in a binary system when condensate shape is known.

142

143 **Measuring droplet shape on flat surfaces**

144 To characterize the shape of condensates typical of *in vitro* reconstitution experiments, we
145 model them physically as sessile fluid droplets on a flat substrate (**Fig. 2a**). In this context,
146 droplet shape is determined at equilibrium by interfacial tension opposing gravitational settling
147 of the denser fluid³³. For droplets smaller than the capillary length $l_c = (\gamma/\Delta\rho g)^{1/2}$, the
148 interfacial tension γ is sufficiently strong to suppress expansion of the interfacial area driven
149 by gravitational effects and the resulting shape is described to an excellent approximation as a
150 spherical cap³³ (**Fig. 2b**). This approximation is valid for most reconstituted condensates,
151 which are typically smaller than our capillary length estimate of $\gtrsim 30 \mu\text{m}$ (**Extended Data Fig.**
152 **1**). In this limit, four parameters suffice to fully characterize droplet shape: droplet radius R ,
153 the position of the droplet center (x_0, y_0) , and the height of the equatorial plane above the
154 substrate, Z_{eq} (**Fig. 2b, Methods**). Importantly, the corresponding projected height function
155 $H(x, y|R, x_0, y_0, Z_{eq})$ has a closed analytic form that we use to determine the refractive index
156 and shape parameters of droplets from QPI images by fitting (**Fig. 2c, Methods**).

157

158 **Experimental validation and conversion from Δn to concentration**

159 To validate the approach experimentally, we use two different reference systems. The first is a
160 well-characterized PEG/Dextran aqueous two-phase system³⁴ for which we can readily
161 measure Δn independently by bulk refractometry (**Methods**). QPI images of Dextran-rich
162 droplets on passivated coverglass and surrounded by a coexisting PEG-rich phase (**Fig. 2d**) are
163 well-modeled as spherical caps (**Fig. 2e**), as evidenced by small and spatially unstructured
164 residuals in the droplet interior following fitting (**Fig. 2f**). For the best fits, Δn is independent
165 of size for three different PEG/Dextran compositions (**Fig. 2g, left**), and approximately
166 symmetrically distributed (**Fig. 2g, right**), indicative of equilibrated phases and uncertainty

167 dominated by statistics rather than systematics, respectively. Crucially, the Δn values extracted
168 from fL-droplets in QPI images are in excellent agreement with those measured independently
169 from 100- μ L volumes of each phase using a digital refractometer (**Fig. 2h**). To validate
170 application of the first-order Born approximation for larger Δn , we used silica microspheres
171 suspended in glycerol-water mixtures as a second reference system, where Δn is set by the
172 glycerol/water ratio. As with the dextran droplets, we recovered the expected shape without
173 bias and find excellent agreement between Δn measurements extracted from QPI images and
174 those expected on the basis of digital refractometry measurements, now over a much larger
175 range (**Fig. 2h, Extended Data Fig. 2**). Taken together, these data demonstrate that the present
176 analysis pipeline extracts accurate geometric and optical measurements of homogeneous
177 sessile droplets from QPI image data for Δn of at least 0.085.

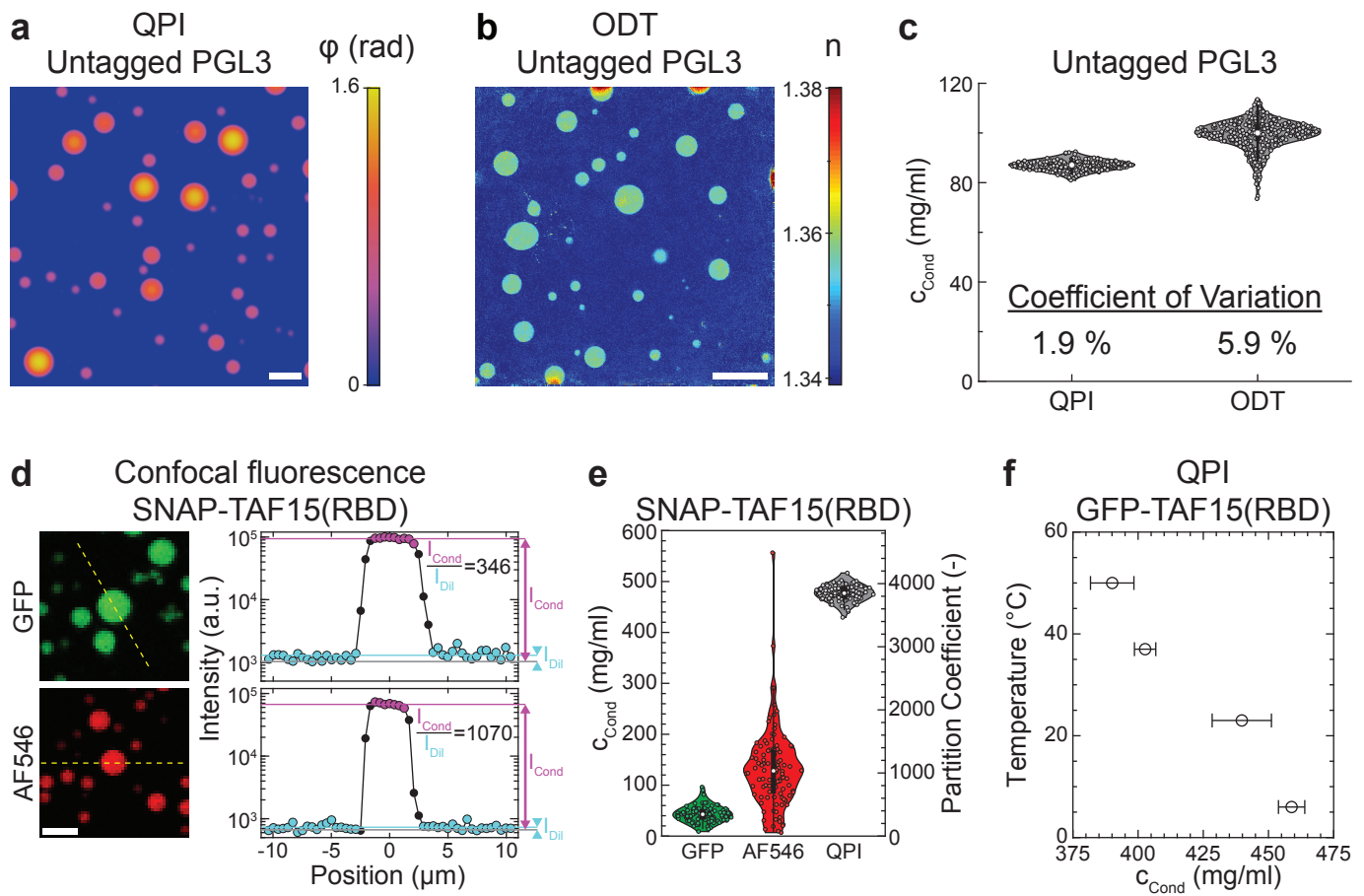
178 Conversion from Δn to compositional differences requires knowledge of the refractive
179 index increments, dn/dc , for each partitioning component. Using bulk refractometry, we
180 determined dn/dc from the concentration-dependence of solution refractive index for several
181 representative (bio)polymers (**Fig. 2i, Extended Data Fig. 3**). In each case, we found excellent
182 linearity over the entire range probed. Importantly, the measured dn/dc value for BSA is
183 consistent with estimates from amino acid sequence³². This validates the use of sequence-
184 based dn/dc estimates in the following, particularly given the impracticality of direct
185 measurement for many recombinant proteins (**Supplementary Note 1**). With dn/dc estimated
186 from protein sequence, Δn measured by QPI, and c_{Dil} measured by standard analytical methods
187 or neglected (**Supplementary Note 3**), Eq. 2 enables calculation of condensed-phase protein
188 concentrations in binary systems.

189

190 **Condensates of native-like proteins**

191 To demonstrate the suitability of our method for condensates reconstituted with native full-
192 length proteins, we first investigated PGL-3, which is a major component of P granules in *C.*
193 *elegans*⁸. PGL-3 forms condensates *in vitro* under low salt⁶. Using QPI, (**Fig. 3a**), we found
194 the concentration in individual PGL3 condensates is symmetrically distributed about a mean
195 of 87.0 ± 0.1 mg/ml (s.e.m., N = 269) (**Fig. 3c**), approximately 1000-fold higher than that in
196 the coexisting dilute phase. The standard deviation of the measured population is only 1.7
197 mg/ml (**Fig. 3c**), yielding a low coefficient of variation (1.9 %) which reflects the high precision
198 of the QPI method as well as the low droplet-to-droplet variation expected near phase
199 equilibrium. Given the impracticality of bulk label-free measurements for this untagged full-

Fig. 3: Label-free composition measurement of multi-domain protein condensates



201 **Fig 3: Label-free composition measurement of multi-domain protein condensates**
202 Quantitative phase, **a**, and refractive index, **b**, images of untagged full-length PGL3
203 condensates acquired by QPI and ODT, respectively. Scalebar is 10 μm . **c**, PGL3
204 concentration measured from individual condensates by QPI (N = 269) or ODT (N = 355). **d**,
205 Confocal fluorescence images of SNAP-TAF15(RBD) condensates doped with either 23 %
206 mEGFP-TAF15(RBD) or 12 % AlexaFluor546-SNAP-TAF15(RBD). Scale bar is 5 μm .
207 Intensity profiles along the dashed yellow lines are shown at right. Gray, cyan, and lavender
208 lines denote the average detector background, dilute-phase intensity, and condensed-phase
209 intensity. **e**, Comparison of SNAP-TAF15(RBD) concentrations in condensates (left) and
210 partition coefficients (right) measured by QPI (N = 119) or confocal fluorescence intensity
211 ratios of mEGFP (N = 107) or AF546 (N = 104). White circles denote medians, thick black
212 bars are the interquartile range, and whiskers extend 1.5x beyond the interquartile range.
213 Protein concentration in the dilute phase is taken to be 1.97 μM . **f**, Temperature-dependence of
214 protein concentration in mEGFP-TAF15(RBD) condensates (i.e. condensed-branch of binodal)
215 measured by QPI. Error bars are s.e.m.
216

217 length protein (**Supplementary Note 1**), we employed Optical Diffraction Tomography (ODT)
218 for comparison (**Fig. 3b,c**). ODT is a related approach recently applied to stress granules^{10,35}.
219 We find ODT to provide a comparable accuracy to QPI, though with reduced precision
220 (**Fig. 3c**).

221 We next formed condensates using constructs derived from full-length FUS and the
222 RNA-binding domain of TAF15, TAF15(RBD), both reported previously in⁷, and measured
223 their composition with QPI. Interestingly, we find these condensates to be much denser than
224 those of PGL3 (**Table 1**), with the 34% polymer volume fraction in TAF15(RBD) condensates
225 comparable to that in protein crystals³⁶. Taken together, these data not only reveal that protein
226 sequence can tune condensate composition over at least a 5-fold range, but also demonstrate
227 that the QPI method enables precise label-free measurements on condensates of full-length
228 proteins. This removes the primary practical barrier preventing study of native full-length
229 proteins that are available only in limited quantities but which are most physiologically
230 relevant.

231

232 **Influence of fluorescent labels**

233 Conventional approaches to study condensates of full-length proteins typically require
234 fluorescent labels, introducing two complications in phase-separating systems. First, large
235 GFP- or SNAP-tags may alter the same phase behavior they are used to measure by shifting
236 the balance of polymer-solvent interactions that drive demixing. Second, fluorophore photo-
237 physics may vary between the starkly different chemical environments presented by the two
238 phases (**Table 1**). We leveraged our label-free method to assess both of these potential effects.
239 In the case of PGL3, we found that fusion to an mEGFP-tag increases the protein mass
240 concentration in the condensed phase by 14 % (**Table 1**). As the tag increases the construct's
241 molecular weight by more than 14 %, this actually corresponds to a decrease in the molar
242 protein concentration, consistent with the tag imparting a modest solubilizing effect.

243 To test for environmentally-sensitive fluorescence, we used scanning confocal
244 microscopy to measure fluorescence in SNAP-TAF15(RBD) condensates doped with either
245 mEGFP- or AlexaFluor546-SNAP-tagged (AF546) constructs (**Fig. 3d, Methods**). The
246 partition coefficient $P \equiv c_{\text{Cond}}/c_{\text{Dil}}$ of ~ 350 obtained from mEGFP fluorescence suggests a
247 condensed-phase concentration of only 43 mg/ml, underestimating the 477 ± 14 mg/ml value
248 we measure with QPI by over 10-fold (**Fig. 3e**). This indicates that the relationship between
249 fluorescence intensity and concentration differs between phases, and we suspect that enhanced
250 quenching from the high protein concentration in the condensed phase is largely responsible

251

Table 1. Compositions of biomolecular condensates in vitro.

Construct	Conditions (T in °C, [salt], pH)	c_{cond} mg/ml ^a	Protein Volume Fraction ^b	Partition Coefficient	Method
PGL3	(25.0, 75 mM, 7.4)	87.0 ± 1.7	0.0649 ± 0.0013	n.d.	QPI
PGL3	(21.5, 87 mM, 7.4)	99.2 ± 5.9	0.0740 ± 0.0044	n.d.	ODT
PGL3-mEGFP	(21.5, 87 mM, 7.4)	113.2 ± 8.6	0.0844 ± 0.0064	n.d.	ODT
SNAP-TAF15(RBD)	(37.0, 100 mM, 7.4)	477.1 ± 13.7	0.3400 ± 0.0098	3850 ^c	QPI
FUS-mEGFP	(21.0, 150 mM, 7.4)	337.3 ± 8.2	0.2395 ± 0.0058	860 ^d	QPI

252

^a Uncertainty represents standard deviation from a population of at least 100 individual condensates

253

^b Fraction of the condensed phase volume occupied by protein, $\phi \equiv c_{\text{Cond}}\bar{v}$; $\bar{v} \approx 0.75$ mL/g for PGL3 constructs and $\bar{v} \approx 0.71$ mL/g for TAF15 and FUS constructs

254

^c $c_{\text{Dil}} = 1.97 \pm 0.09$ μM , $M_w = 62.92$ kDa; ⁷

255

^d $c_{\text{Dil}} = 4.87 \pm 0.48$ μM , $M_w = 80.38$ kDa; ⁷

256

257

258 for the decreased quantum yield we infer there ³⁷. Surprisingly, assessing partitioning by
259 fluorescence of the more solvent-accessible AlexaFluor546-labeled construct underestimates
260 the concentration by 3.6-fold (**Fig. 3e**). The differential sensitivity we see with different
261 fluorophores suggests that brightness may vary for each dye/condensate pair and be
262 challenging to correct for *a priori*. Taken together, these data demonstrate that fluorescent
263 labels compromise condensate composition measurements in two distinct ways, sometimes
264 dramatically, underscoring the importance of label-free approaches like QPI.

265

266 **Temperature-dependent phase behavior**

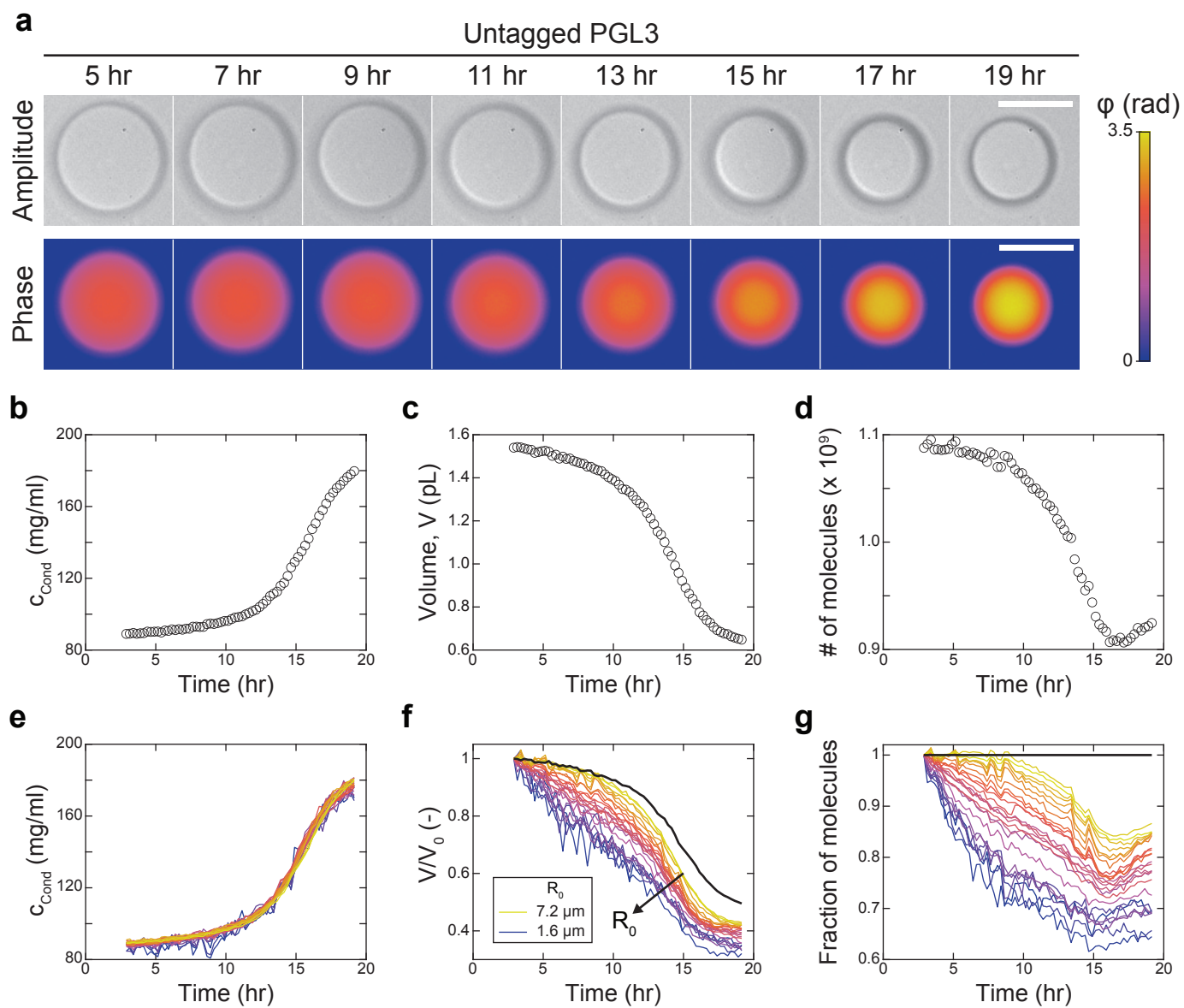
267 Biomolecular condensates are intrinsically temperature-dependent as thermodynamic phases,
268 making temperature an important control parameter subject to evolutionary selection ³⁸. To test
269 whether we could detect temperature-induced composition variation with QPI, we analyzed
270 phase images of TAF15(RBD) condensates acquired at temperatures between 5 and 50 °C set
271 with a custom temperature stage (**Methods**, ³⁹). After accounting for the temperature-
272 dependence of optical constants in Eq. 1 (**Extended Data Fig. 4**), we find that the condensed-
273 phase protein concentration decreases significantly from ~ 460 to ~ 390 mg/ml with increasing
274 temperature (**Fig. 3f**). This is indicative of an upper-critical solution temperature (compare to
275 **Fig. 1a**), as has been reported for several other ^{23,40}, though not all ³⁸, RNA-binding proteins.
276 Finally, the dry objective lenses used for QPI enable fast temperature equilibration by avoiding
277 direct coupling of their thermal mass to the temperature stage.

278

279 **Complex aging dynamics in binary systems**

280 Motivated by recent work demonstrating that the mechanical properties of many protein
281 condensates undergo an aging process ^{41-43,26}, we hypothesized that there may be a
282 corresponding change in composition as condensates age. To this end, we used QPI to measure
283 the composition of individual PGL3 condensates over 20 hours (**Fig. 4**). During this time
284 period, we observed droplets to noticeably shrink (**Fig. 4a, top, Supplementary Video 1**), as
285 previously shown ²⁶. While the shrinkage would be apparent by simple brightfield imaging,
286 QPI indicated that the optical phase shift also increased with time, despite the reduction in
287 droplet size (**Fig. 4a, bottom**). By fitting the QPI data as before, we were able to precisely
288 measure the composition (**Fig. 4b**) and volume (**Fig. 4c**) of individual condensates over this
289 timeframe, revealing surprisingly coordinated dynamics. From these concentration and volume
290 data, we calculated the number of proteins in the condensate (**Fig. 4d**) and found that the nearly
291 2-fold concentration increase was approximately balanced by a volume decrease, such that the

Fig. 4: QPI reveals complex aging dynamics in binary systems



293 **Fig 4: QPI reveals complex aging dynamics in binary systems**
294 **a**, Timelapse of untagged PGL3 condensate (top, QPI amplitude; bottom, QPI phase). Scale
295 bar 10 μm . Concentration **b**, volume **c**, and number of protein molecules in the condensate **d**
296 for the example in **a**. Time is relative to induction of phase separation. **e**, Time-dependence of
297 concentration is identical for $N = 25$ differently sized condensates. **f**, Normalized volume varies
298 continuously with initial condensate size R_0 . Initial shrinkage rate decreases with increasing
299 R_0 . **g**, Fraction of molecules in 25 individual condensates over time. Thick black lines in **f,g**
300 show volume and molecule count dynamics if protein mass were conserved inside condensates.
301

302 total number of protein molecules in the condensate decreased by only 15 %. These
303 observations indicate that the condensate necessarily expelled a significant amount of solvent
304 while aging.

305 To quantify whether this near cancellation was serendipitous for this particular
306 condensate, we analyzed the dynamics of 24 additional condensates with a range of initial sizes
307 over the same period (**Fig. 4e-g**). Strikingly, we found that the kinetics and extent of
308 concentration increase were identical for all condensates, independent of size (**Fig. 4e**). In
309 contrast, the kinetics and extent of the volume decrease both showed systematic size
310 dependencies, with smaller condensates losing volume faster and to greater extent than larger
311 condensates (**Fig. 4f**). As a result, the fraction of molecules retained shows a marked
312 dependence on condensate size, with larger condensates retaining more molecules (**Fig. 4g**).
313 We speculate that the size dependence in the volume kinetics may stem from Ostwald ripening
314 operating in parallel with an additional as yet unknown process driving the contraction and
315 water expulsion. Taken together, these data demonstrate the suitability of QPI to monitor the
316 composition of many individual droplets in parallel, providing insight into the complex
317 interplay between the physical processes driving ripening and aging.

318

319 **Measuring binodals and tie-lines with an arbitrary number of components**

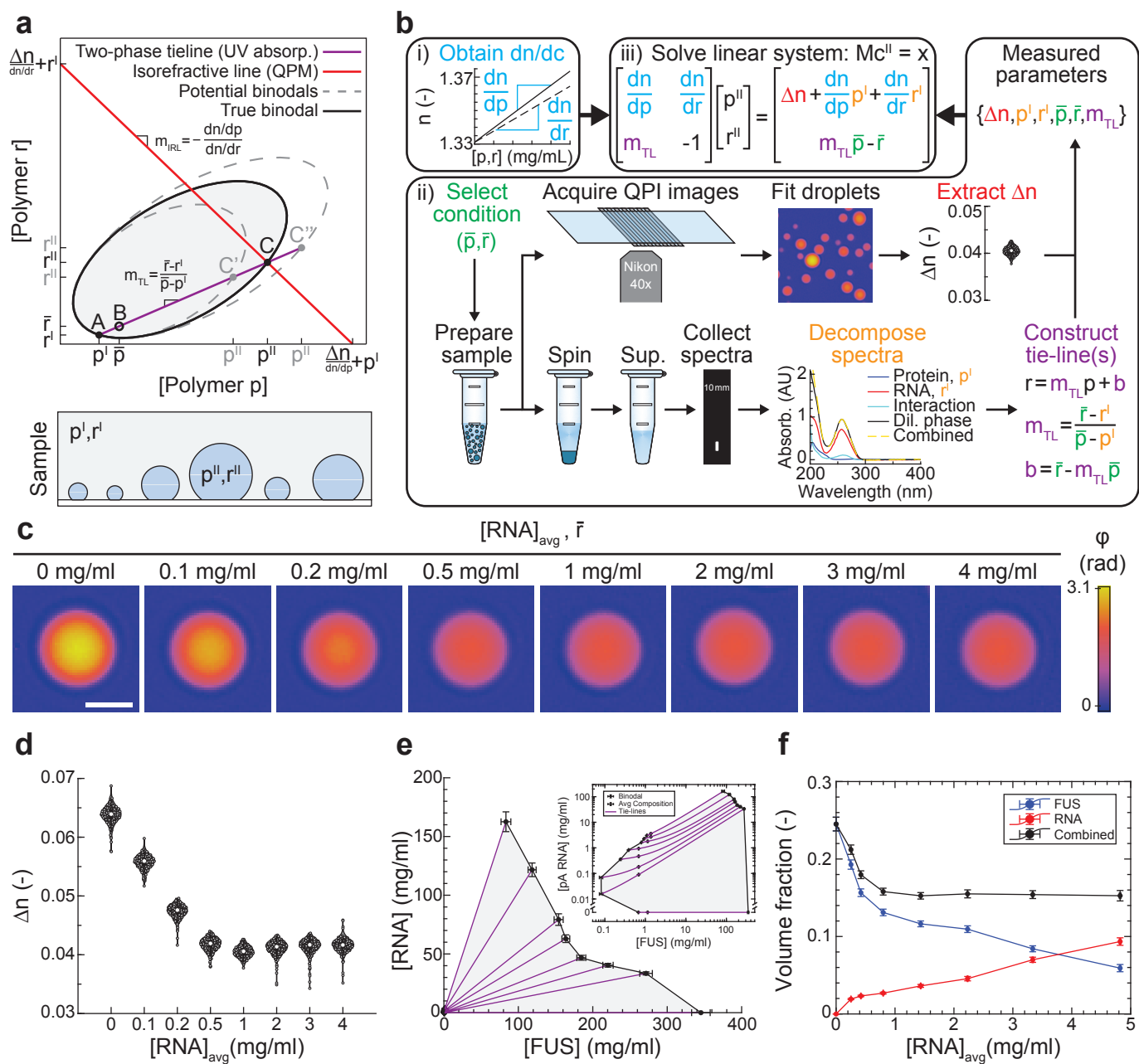
320 As condensates in cells are typically enriched in several distinct biomolecular species, we next
321 asked whether QPI could specify the composition of reconstituted condensates with multiple
322 components. In the linear approximation (**Extended Data Fig. 5**), the refractive index
323 difference between two phases with N solutes is

$$324 \quad \Delta n \approx \sum_{i=1}^N \frac{dn}{dc_i} \Delta c_i, \quad (\text{Eq. 3})$$

325 where Δc_i is the concentration difference of the i^{th} component between the two phases. While
326 knowledge of Δn constrains Δc to a single value in the binary systems studied above, the
327 challenge for systems with multiple solutes is that Δn constrains the Δc_i only to an $(N-1)$ -
328 dimensional manifold populated by compositions of equal refractive index. For a ternary
329 system with $N = 2$ solutes and 1 solvent, for instance, this manifold can be visualized as a line
330 in the (c_1, c_2) -plane (**Fig. 5a**). As all compositions along this isorefractive line are compatible
331 with the measured Δn , additional relationships between the Δc_i are required to uniquely specify
332 condensate composition.

333 Here, we take advantage of the fact that a tie-line connects the total system composition
334 averaged over both phases, $(\bar{c}_1, \bar{c}_2, \dots, \bar{c}_N) \equiv \bar{c}$, to the compositions of the coexisting phases \mathbf{c}^l

Fig. 5: Composition determination of multi-component biomolecular condensates



336 **Fig 5: Composition determination of multi-component biomolecular condensates**
337 **a**, Top: Schematic of multi-component measurement approach illustrated for a model ternary
338 system. Condensate composition (p^{II}, r^{II}) is determined by the intersection of the tie-line with
339 the line of constant refractive index (isorefractive line). Bottom: Schematic of coexisting multi-
340 component phases. **b**, Workflow to obtain all parameters in the system of linear equations. i)
341 Refractive index increments are determined once for each partitioning component. ii) For each
342 tested composition (\bar{p}, \bar{r}) in the two-phase regime, Δn is measured with QPI and the dilute
343 phase composition (p^I, r^I) is inferred from decomposition of UV-VIS absorbance spectra. The
344 points (\bar{p}, \bar{r}) and (p^I, r^I) suffice to define the tie-line, whose slope m_{TL} is the final required
345 parameter to solve the linear system, iii). **c**, QPI images of FUS/RNA condensates for a range
346 of RNA concentrations \bar{r} . Scalebar is 3 μm . **d**, Measured Δn distributions for the samples in **c**.
347 **e**, Experimentally-determined ternary phase diagram. Inset shows the same data on loglog axes.
348 Error bars denote standard deviation for dilute-phase and average concentrations, and error
349 propagation via Jacobian for condensed-phase concentrations. **f**, Polymer volume fractions in
350 the condensed phase as a function of \bar{r} with $\bar{p} = 2$ mg/ml. Error bars correspond to the
351 uncertainty in condensed-phase concentration rescaled by polymer partial specific volumes.
352

353 and \mathbf{c}^{II} located on the $(N-1)$ -dimensional dilute and condensed binodal manifolds,
354 respectively. For ternary systems, the binodals can be visualized as bounded curves in the
355 (c_1, c_2) -plane (**Fig. 5a**). Mass conservation guarantees that tie-lines are straight (**Fig. 5a**,
356 **Supplementary Note 4**). Crucially, this provides $N-1$ linearly independent constraints, which
357 can be seen by noting that projections of the tie-line in each of the $N-1$ $(c_1, c_{i \neq 1})$ -planes must
358 all be straight. In principle, tie-line constraints of the form $c_i = m_{1i}c_1 + b_{1i}$ where $m_{1i} =$
359 $(\bar{c}_i - c_i^I)/(\bar{c}_1 - c_1^I)$ and $b_{1i} = \bar{c}_i - m_{1i}\bar{c}_1$ for $i \neq 1$ can be obtained from knowledge of overall
360 sample conditions, $\bar{\mathbf{c}}$, and composition measurements of the abundant dilute-phase c_i^I using
361 traditional approaches from analytic chemistry (**Supplementary Notes 3,5**). Combined with
362 Eq. 3, these form a linear system of N equations of the form $M\mathbf{c}^{II} = \mathbf{x}$, where the matrix M and
363 vector \mathbf{x} contain measured quantities (see **Fig. 5b**, **Supplementary Note 5** for explicit
364 expressions for ternary and $(N+1)$ -component systems, respectively). By solving this system
365 of equations, the composition of the multi-component condensate is written in terms of known
366 optical quantities and concentrations as

367
$$c_i^{II} = \Delta n M_{i1}^{-1} + c_i^I, \quad (\text{Eq. 4})$$

368 where M_{i1}^{-1} are elements of the system's matrix inverse (**Supplementary Note 5**). Thus, by
369 leveraging knowledge of tie-lines to provide the missing the constraints, this method is, in
370 principle, capable of resolving the composition of biomolecular condensates with an arbitrary
371 number of components.

372

373 **Phase diagram for ternary system with full-length FUS protein and RNA**

374 To validate this approach, we used poly(A) RNA and full length FUS-mEGFP, which localizes
375 to RNA-rich stress granules in eukaryotes¹⁰, as solutes in a model ternary system ($N = 2$).
376 Following the workflow in **Fig. 5b**, we prepared systems in the two-phase region for a range
377 of total RNA concentrations. To obtain the dilute-phase composition, we decomposed UV
378 absorbance spectra of the dilute phase into protein and RNA contributions (**Fig. 5b**, **Methods**).
379 Combined with the system average compositions, the decomposed spectral data produce a set
380 of physically compatible tie-lines (**Extended Data Fig. 6**). To obtain Δn , we analyzed QPI
381 data (**Fig. 5c**), finding that Δn decreases and saturates with increasing total RNA (**Fig. 5d**).
382 Using these data as inputs in Eq. 4 (**Fig. 5b**), we calculated the corresponding points on the
383 condensed binodal branch and plotted these together with the dilute binodal and tie-lines as a
384 full phase diagram (**Fig. 5e**). Reassuringly, this phase diagram captures the re-entrant behavior
385 with increasing RNA inferred previously in related systems without actually measuring the

386 phase boundary^{44,45}. In addition to connecting variation in system average composition directly
387 to its consequences on the condensate, which was seldom accessible previously²¹, this phase
388 diagram exposes surprising features in the condensed binodal branch, including a kink and
389 linear section (**Fig. 5e**). The ability of this method to resolve the molecular composition of
390 multi-component condensates reveals that rising RNA concentrations are compensated by
391 decreasing protein concentrations such that a constant polymer volume fraction is maintained
392 near cytoplasmic levels (**Fig. 5f**), which would have been challenging to infer using
393 conventional techniques.

394

395

DISCUSSION

396 Our results show that the present QPI-based method enables quantitative composition
397 measurements of biomolecular condensates reconstituted with full-length proteins in binary
398 and multi-component mixtures. Our finding that a common fluorescent tag can significantly
399 alter condensate composition (**Table 1**) highlights the need for label-free measurement
400 approaches like QPI. As a microscopic method, QPI offers several advantages over traditional
401 label-free strategies based on bulk measurements. The first and most dramatic of these is the
402 ~1000-fold reduction in sample requirements, which removes the primary barrier to
403 measurements on condensates reconstituted from native full-length proteins (**Fig. 3a,b**).
404 Second, whereas time-resolved measurements of composition in response to changing solution
405 conditions, temperature, or intrinsic sample dynamics are challenging with bulk approaches,
406 QPI's compatibility with open samples and dry objectives makes it easy to record sample
407 dynamics with second-scale time resolution (**Fig. 4**) and in response to environmental changes
408 (**Fig. 3f**). Third, measuring composition of micron-sized condensates *in situ* provides access to
409 information like size-dependent composition (**Fig. 2g**), homogeneity (**Fig. 2f**), and dynamics
410 (**Fig. 4e-g**) that are not available with bulk techniques. Finally, we note that the high precision
411 demonstrated here with QPI not only enables the method to resolve subtle compositional
412 differences (**Table 1**) and unexpected binodal features (**Fig. 5f**) with high confidence, but could
413 also serve to constrain competing thermodynamic models of condensate formation^{22,7,46,24,47,25}.

414 An important benefit of the present method is its ability to disentangle the composition
415 of multi-component biomolecular condensates. All endogenous condensates are expected to
416 contain multiple components, with some of the best-characterized known to house dozens⁸⁻¹⁰.
417 Knowledge of component identity and quantity will be essential for design and interpretation
418 of increasingly faithful reconstitution experiments as well as studies of chemical reactions in

419 synthetic condensates that account for reacting species. Here, we validated our methodology
420 by measuring the full phase diagram for a ternary mixture of full-length FUS protein and RNA,
421 including the dilute- and condensed-binodal branches as well as tie-lines (**Fig 5f**). We note that
422 three pieces of information, tie-lines along with both binodals, are strictly required to physically
423 relate the compositions of coexisting phases to the average composition specified in
424 experiments, and that no other methods suitable for low-yield proteins provide all three.
425 Further, we proved mathematically that the proposed methodology can, in principle, resolve
426 the composition of condensates containing an arbitrary number of distinct molecular
427 components (**Supplementary Note 5**). Whether partitioning of a particular species can be
428 resolved is determined primarily by the sensitivity and precision of the dilute-phase detection
429 method employed (**Extended Data Fig. 7**). We emphasize that our methodology is agnostic to
430 the choice of dilute-phase detection method. This flexibility allows experimenters to select or
431 combine established analytic approaches best-suited for the molecules used. In particular,
432 mass-spectrometry can resolve complex mixtures with 100s or 1000s of components and
433 distinguish between protein some PTM-states ⁴⁸.

434 In future applications of this method, there are three classes of practical considerations
435 that must be kept in mind. The first concerns condensate size. Though QPI measures refractive
436 index robustly for droplets over the size-range most commonly encountered in reconstitution
437 experiments, from a few to a few 10s of microns, systematic errors are incurred due to
438 scattering and gravitational settling for sufficiently small and large droplets, respectively. We
439 anticipate that additional development of fitting routines to account for these physical effects
440 can further extend the size range for reliable measurements ^{49,50}. The second consideration
441 involves treating the refractive index of a mixture as a linear sum of contributions from its
442 components (see **Eq. 3, Supplementary Note 2**). This is a very good approximation for protein
443 solutions over a wide range ³⁰, though higher-order terms could potentially contribute for some
444 molecules ⁵¹. In the cases we checked, we found the linear sum to describe the refractive index
445 of multi-component mixtures accurately to within a few % (**Extended Data Fig. 5**). We also
446 note that while contributions from PTMs are currently neglected when estimating protein
447 refractive index increments ³², which are the coefficients in the linear sum, this could be readily
448 addressed in the future with molar refractivity measurements of modified amino acids in
449 solution ⁵². This could improve accuracy for condensates containing highly-modified proteins.
450 The third consideration is in regard to measurements in cells. Though our QPI-based method
451 is best-suited for reconstituted condensates, QPI and related techniques like ODT can provide
452 some information on cellular condensates whose refractive index differs sufficiently from the

453 surrounding material ^{53,31,35}. For condensates with sufficient contrast, reconstruction of
454 binodals and tie-lines would require knowledge of molecular abundances in individual cells as
455 well as the coexisting phase. Absent this, phase-based imaging data can still provide a
456 quantitative measure of the average macromolecular mass difference between phases *in vivo*,
457 which may be particularly informative in the context of perturbations.

458 As composition ultimately influences all other condensate properties and associated
459 cellular functions, we anticipate a central role for this method in addressing many pressing
460 biological questions. Measuring condensate composition as the abundance of individual
461 components are systematically varied will reveal the thermodynamic contributions of these
462 molecules to the phase, potentially clarifying the biological function of individual components.
463 We anticipate that correlating composition with other physical properties like viscoelasticity,
464 interfacial tension, and dielectric constant will likewise provide insight into condensate
465 function. By providing a ground-truth with which to calibrate fluorophore behavior, we expect
466 that this method will enable the use of dyes to both follow reactions localized to condensates
467 as well as quantitatively probe the chemical environment within condensates. The latter will
468 likely be essential to understand and potentially tune the partitioning of therapeutic drugs into
469 condensates in treatment of diseases like cancer ⁵⁴.

470

471

MATERIALS AND METHODS

472 **Sample preparation.** Recombinant protein constructs used in this work were purified and
473 stored as described previously ^{6,7}. To induce phase separation, we mixed protein in high-salt
474 storage buffer (300 mM KCl for PGL3 constructs, 500 mM KCl for TAF15 and FUS
475 constructs) with storage buffer lacking monovalent salt, “Dilution Buffer”, to reach the desired
476 final salt concentration. Generally, an aliquot of Dilution Buffer was supplemented to 1 mM
477 with fresh DTT prior to each day’s experiments. After induction of phase separation, dilute
478 phase was obtained by centrifugation at $RCF = 20,800 \times g$ for 30 min in a tabletop centrifuge
479 (Centrifuge 5417 R, Eppendorf) pre-equilibrated at the desired temperature. For control
480 measurements, 10- μ m silica microspheres were purchased from Whitehouse Scientific
481 (Waverton, UK), and glycerol-water-mixtures were prepared by weight to the desired refractive
482 index. Bead-containing dispersions were prepared by gently dipping a 10- μ L pipette tip into a
483 stock of dry beads, transferring the pipette tip to a 40 μ L volume of glycerol-water mixture,
484 and pipette mixing to disperse. Aqueous two-phase systems with PEG-35k (Sigma) and

485 Dextran T500 (Pharmacosmos) were prepared as described previously³⁴. BSA was purchased
486 from Sigma and used without further purification.

487 **Quantitative phase imaging and analysis.** QPI measurements were performed using a
488 coherence-controlled digital holographic microscope (Q-Phase, Telight (formerly TESCAN),
489 Brno, CZ) based on the set-up in²⁸. Most data were acquired on a Generation-1 instrument
490 with a tungsten-halogen bulb as lightsource, though some data were acquired on a Generation-
491 2 instrument with a 660-nm LED as lightsource. In each case, the holography lightsource was
492 filtered by a 10-nm bandwidth notch filter centered at 650 nm. All measurements were
493 performed with 40x dry objectives (0.9 NA, Nikon) except those for SNAP-TAF15(RBD)
494 reported in **Fig. 3f**, for which 20x dry objectives were used. In all cases, the condenser aperture
495 was set to an NA of 0.30. Immediately following phase separation, ~ 5 μ L of sample was
496 loaded into a temperature-controlled flowcell, sealed with two-component silicone glue
497 Twinsil (Picodent, Wipperfurth, DE), and allowed to settle under gravity for ~ 10 minutes prior
498 to data collection. Flowcells were constructed with a 30x24x0.17 mm³ PEGylated coverslip
499 and a 75x25x1 mm³ sapphire slide as bottom and top surfaces, respectively, using parafilm
500 strips as spacers. Proportional-integral-derivative (PID)-controlled Peltier elements affixed to
501 the sapphire slide enabled regulation of flowcell temperature, as previously described³⁹. The
502 sapphire, coverslip, and spacers were adhered by heating the assembled flowcell to 50 °C for
503 2-5 min, then returning to the desired temperature for the first measurement, typically to 20 °C.
504 For each sample, hologram z -stacks ($dz = 0.2 \mu\text{m}$, first plane typically near the coverglass
505 surface) were acquired for several fields of view. SophiQ software (Telight, Brno, CZ) was
506 used to construct amplitude and compensated phase images from the raw holograms. Pixels in
507 the phase images are 0.157 μm per side for the 40x, and pixel intensities are in units of radians.
508 To aid interpretation by persons with red/green color perception deficiencies, phase images are
509 displayed using the Ametrine colormap⁵⁵.

510 All phase images were analyzed in MATLAB using custom code. For each z -plane,
511 compensated phase images were first segmented to identify individual droplets. To determine
512 the background phase value, φ_0 , the image's pixel intensity histogram was fit to a Gaussian,
513 and the Gaussian center taken as φ_0 . Pixel intensities $\varphi \geq n_{sig}\sigma_\varphi$ are considered above
514 threshold, where σ_φ is the standard deviation extracted from the Gaussian fit. Typically,
515 $n_{sig} = 5$. A binary mask was generated with this threshold and individual objects were identified
516 using the MATLAB function `bwconncomp.m`. For each object, a region of interest slightly

517 larger than the object's bounding box was fit twice to phase functions of the form given by Eq.
518 (1) in the main text. First, we fit using the projected height of a sphere,

$$519 H_{sphere}(x, y|R, x_c, y_c) = \Theta(R^2 - (x - x_c)^2 - (y - y_c)^2) \sqrt{R^2 - (x - x_c)^2 - (y - y_c)^2},$$

520 in order to obtain estimates for the parameters $\Delta n, R, x_c, y_c$, where $\Theta(x)$ is the Heaviside
521 function. These estimates were then used to initialize a fit to a regularized version of Eq. (1),

$$522 \Delta\varphi_{Reg}(x, y) = \frac{2\pi}{\lambda} \Delta n H_{cap}(x, y|R, x_c, y_c, Z_{eq}) + \varphi_0 + A(Z_{eq}, R),$$

523 using the projected height of a spherical cap,

$$524 H_{cap}(x, y|R, x_c, y_c, Z_{eq}) = \sqrt{R^2 - (x - x_c)^2 - (y - y_c)^2} \left(1 + \Theta(Z_{eq}^2 + (x - x_c)^2 + (y - y_c)^2 - R^2) \right) \Theta(R^2 - (x - x_c)^2 - (y - y_c)^2) + Z_{eq} \Theta(R^2 - Z_{eq}^2 - (x - x_c)^2 - (y - y_c)^2).$$

526 The regularization is given by $A(Z_{eq}, R) = A_0(Z_{eq} - R)^2 \Theta(Z_{eq} - R)$ with $A_0 = 10^5$ and φ_0
527 fixed at the value obtained from the pixel intensity histogram fit. After all z-planes were
528 processed, the objects were tracked through z using track.m
529 (<https://site.physics.georgetown.edu/matlab/index.html>). For each tracked object, the
530 representative fit parameters are taken as those from the fit with the highest Adj. R^2 value,
531 which are typically in the plane acquired nearest to the equatorial plane of a given droplet. The
532 particle list was then automatically filtered for fit quality (typically retaining only Adj. R^2 -
533 values > 0.95) and overlap with dead-pixels on the detector. Droplets with irregular wetting or
534 that are not isolated in z (i.e. are situated beneath other droplets in solution) are removed
535 manually following inspection of the raw data.

536 **Optical Diffraction Tomography.** ODT measurements were performed using a custom-built
537 microscope employing a 532-nm laser, as described previously⁵⁶. Tomogram reconstruction
538 and image analysis was performed as described previously^{57,10}.

539 **Confocal Fluorescence Microscopy and Analysis.** Confocal imaging was performed on an
540 inverted Zeiss LSM880 point-scanning confocal microscope with a 40x water-immersion
541 objective (1.2 NA, C-Apochromat, Zeiss) at room temperature. mEGFP was excited with a
542 488-nm argon laser and emission detected with a 32-channel GaAsP photomultiplier tube
543 (PMT) array set to accept photon wavelengths between 499 and 569 nm. AlexaFluor546 was
544 excited with a 561-nm diode-pumped solid-state laser and emission detected between 570 and
545 624 nm with the same spectral PMT array. For both fluorophores, the confocal pinhole
546 diameter was set to 39.4 μm , corresponding to 0.87 and 0.96 Airy Units for mEGFP and
547 AlexaFluor546, respectively. For each field of view, scanning was performed with a lateral
548 pixel size of 0.415 μm and z -stacks acquired with a spacing of 0.482 μm .

549 All confocal fluorescence images were analyzed in MATLAB using custom code.
550 Partition coefficients of fluorescently-labeled species into condensates are estimated on the
551 basis of the fluorescence intensity along a line-scan through the droplet center. The analysis
552 pipeline begins with determining the location of each condensate and an appropriate line-scan
553 orientation angle. To determine lateral positions of condensates in each field of view, a z-plane
554 was selected slightly above the coverglass such that even small droplets appeared bright.
555 Following convolution with a 2D Gaussian ($\sigma_x = \sigma_y = 0.5$ pixels) to suppress shot noise, a
556 threshold of $I_{thresh} = \max(I(x, y)) / 2$ was applied to obtain a binary mask. The lateral
557 positions and approximate sizes of objects were determined from the mask with
558 `bwconncomp.m`. Only the largest ~120 objects for each condition were analyzed further. For
559 each object, partition coefficients were calculated using the z-plane for which the mean
560 intensity in a 5-pixel-radius disk concentric with the object was greatest. Line-scans were 51
561 pixels long, concentric with the object, and averaged over a width of 3 pixels. Suitable line-
562 scan orientations were determined in a semi-automated manner by superimposing reference
563 lines rotated through 15° increments on each object and manually selecting an orientation that
564 best avoided neighboring objects. Objects for which no suitable line-scan orientation could be
565 found were discarded.

566 Line-scans for each droplet were automatically subdivided into three domains,
567 corresponding to pixels in the dilute phase, the condensed phase, or the exclusion zone. The
568 positions of the left and right dilute/condensed interfaces are estimated as those at which the
569 intensity profile reaches its half-maximal value above detector background I_{Bkgd} (see below).
570 To reduce artefacts stemming from the finite point-spread function of the microscope, pixels
571 within the greater of 1 pixel or $l_{EZ} = 1.22\lambda / (2NA)$ on either side of the half-maximum were
572 excluded from the analysis. Remaining profile pixels outside the droplet were averaged to give
573 I_{Dil} , while profile pixels inside are averaged to give I_{Cond} . The partition coefficient for each
574 object was calculated according to

575
$$P = \frac{I_{Cond} - I_{Bkgd}}{I_{Dil} - I_{Bkgd}},$$

576 where I_{Bkgd} is the average of all pixels in a background image acquired immediately following
577 the fluorescence z-stack. Background images were acquired with the light source blocked to
578 measure the contribution of detector noise to the signal.

579 **Bulk Refractometry.** Data in Fig. 2i were acquired at $\lambda = 653.3$ nm and 21 °C with a DSR-L
580 multi-wavelength refractometer (Schmidt + Haensch, Berlin) using a 200- μ L sample volume.
581 All other bulk refractive index measurements were acquired at $\lambda = 589.3$ nm with a J457

582 refractometer (Rudolph Research Analytical, Hackettstown, NJ). The refractive index of
583 glycerol/water mixtures was adjusted from $\lambda = 589.3$ to 650 nm using empirical dispersion
584 relations for distilled water, $n_{Water}(\lambda)$ ⁵⁸, and glycerol, $n_{Glycerol}(\lambda)$ ⁵⁹ according to

$$585 \quad n_{Mix}(\lambda) = w_{Glycerol}n_{Glycerol}(\lambda) + (1 - w_{Glycerol})n_{Water}(\lambda).$$

586 The glycerol weight fraction in the mixture was calculated from the refractive index
587 measurement of the mixture at 589.3 nm as

$$588 \quad w_{Glycerol} = (n_{Mix}(\lambda) - n_{Water}(\lambda)) / (n_{Glycerol}(\lambda) - n_{Water}(\lambda)) \Big|_{\lambda=589.3}.$$

589 **Bead porosity models.** The two models used to account for the porosity p of the silica
590 microspheres (Fig. 2h, Extended Data Fig. 2) are a weighted linear sum, $\Delta n = pn_{Silica} +$
591 $(1 - p)n_{Water}$ (simple model), and a more detailed model,

$$592 \quad \Delta n = \left(\frac{1 + 2(1 - p)f(n_{Silica}) + 2pf(n_{Mix})}{1 - (1 - p)f(n_{Silica}) + pf(n_{Mix})} \right)^{1/2} - n_{Mix}$$

593 based on the Lorentz-Lorenz relation⁶⁰, wherein

$$594 \quad p = \frac{f(n_{Silica}) - f(n_{Microsphere})}{f(n_{Silica}) - f(n_{GlycerolWaterMixture})}$$

595 with $f(n) \equiv (n^2 - 1)/(n^2 + 2)$.

596 **Calculation of dn/dc , \bar{v} and polymer volume fraction.** The refractive index increment and
597 partial specific volume were estimated for each protein construct using the calculator tool
598 within SEDFIT³² and the protein sequences listed in the SI. The partial specific volume of
599 0.5773 mL/g for poly(A) RNA was estimated using consensus volumes per base from⁶¹ and
600 assuming a typical chain length of 500 bases. The partial specific volumes of 0.8321 and 0.6374
601 mL/g for PEG-35k and Dextran-500k, respectively, were taken from³⁴. Polymer volume
602 fraction (Fig. 5f) for polymer i is given by $\phi_i = c_{Cond}\bar{v}$.

603 **Calculations for aging systems.** Volumes of individual aging condensates (Fig. 4c,f) were
604 calculated as $V = \frac{4}{3}\pi R^3$. The number of molecules in each condensate (Fig. 4d,g) were
605 calculated as $N(t) = c(t)V(t)$. Given $c(t)$, the relative volume change expected if $N(t) =$
606 $N(0)$ is given by $V(t)/V(0) = c(0)/c(t)$ (Fig. 4f, black line).

607 **UV-Vis spectroscopy.** Absorption spectra of dilute-phase and reference samples for the
608 FUS/RNA system (Fig. 5) were collected on an NP-80 spectrophotometer (IMPLEN,
609 München). All spectra were acquired at room temperature over $\lambda \in [200 \text{ nm}, 900 \text{ nm}]$. For
610 each raw spectra $\tilde{S}(\lambda)$, a linear fit on $\lambda \in [550 \text{ nm}, 750 \text{ nm}]$ was used to determine a baseline
611 correction, $S_{BL}(\lambda)$. Corrected spectra are given by $S(\lambda) = \tilde{S}(\lambda) - S_{BL}(\lambda)$. At least 3 replicate

612 spectra were acquired for each condition and averaged following baseline correction to give
613 the final representative spectra. The uncertainty in the spectra at each wavelength was
614 estimated as the standard deviation of the corrected replicates. Dilute-phase spectra were
615 demixed (Fig. 5b) into a weighted sum of three contributions

$$616 \quad S_{Dil}(\lambda) = p^l S_p(\lambda) + r^l S_r(\lambda) + p^l r^l a_{int} S_{int}(\lambda),$$

617 where (p^l, r^l) are the protein and RNA concentrations in the dilute phase. S_p and S_r are
618 reference spectra for protein and RNA, respectively. The final term captures the effect of
619 protein-RNA interactions on the absorbance of a mixture, which could physically stem from
620 binding-induced changes in extinction coefficients. Reference spectra for the interaction was
621 calculated from spectra of a protein/RNA mixture of known composition (p, r) in the 1-phase
622 regime according to $S_{int} = S(p, r) - pS_p - rS_r$. The parameter a_{int} captures the
623 approximately linear increase of S_{int} with p . The same value of a_{int} was used to demix all
624 dilute-phase spectra. The dilute-phase concentrations p^l, r^l were therefore the only free
625 parameters for the demixing.

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AUTHOR CONTRIBUTIONS

PMM, JP, AAH, and JB conceived the project. PMM conceived and developed the multi-component measurement approach and derived the analytical solution. PMM designed and performed QPI, refractometry, spectroscopy, and fluorescence microscopy measurements, developed the analysis pipelines for these data types, and performed the formal analysis. KK and PMM designed and performed ODT measurements. KK analyzed ODT data. MR-G purified multiple constructs and articulated essential distinctions related to the handling of IDRs and multi-domain proteins. JB, AAH, and JG supervised the work. PMM and JB wrote the paper with input from all authors.

COMPETING INTERESTS

AAH is a founder of Dewpoint Therapeutics and a member of the board as well as a shareholder in Caraway Therapeutics. All other authors have no competing interests.

DATA AVAILABILITY

Data generated and analyzed supporting the findings of this Article will be made available by the Authors upon reasonable request.

CODE AVAILABILITY

Custom code generated supporting the findings of this manuscript will be made available by the Authors upon reasonable request.

SUPPLEMENTARY INFORMATION

- Note 1: Requirements of bulk measurements
- Note 2: Linear approximation to refractive index of mixtures
- Note 3: Measurement of c_{DI}
- Note 4: Requirement that tie-lines are straight
- Note 5: Derivation of condensate composition for multi-component systems
- Supplementary References
- Table S1: Protein constructs used
- List S1: List of protein sequences used

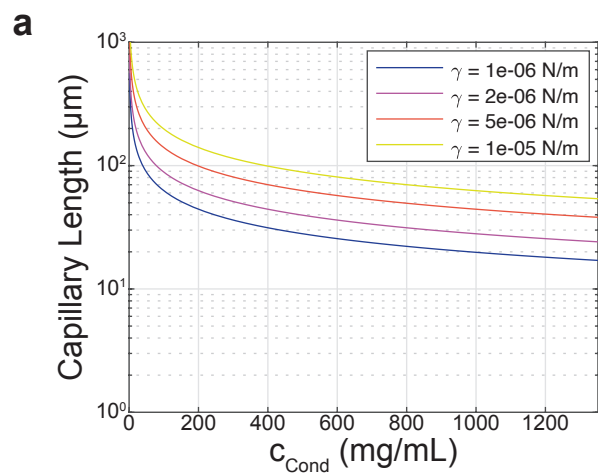
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EXTENDED DATA FIGURES AND CAPTIONS

Extended Data Fig. 1: Estimate of capillary length for biomolecular condensates

a, Capillary length as a function of the condensed-phase polymer mass concentration. The capillary length increases with increasing interfacial tension, so we plot traces for different values of interfacial tension. From bottom to top, interfacial tensions are 1, 2, 5, and 10 $\mu\text{N/m}$. This spans the range of tensions reported for PGL-3 condensates by ⁶². For a given droplet density and interfacial tension, the spherical cap approximation for the droplet shape is valid so long as the droplet size is less than the capillary length. In the case of PGL-3, our density measurements of ~ 90 mg/ml indicate a capillary length of 67 μm at the lowest interfacial tension, which is much larger than the 1-8 μm radii of the droplets. Although the capillary length is reduced to ~ 30 μm for the higher ~ 400 -500 mg/ml densities we measure for TAF15(RBD) condensates, this length is still much larger than the 0.67-3.2 μm radii of those condensates analyzed in this work.

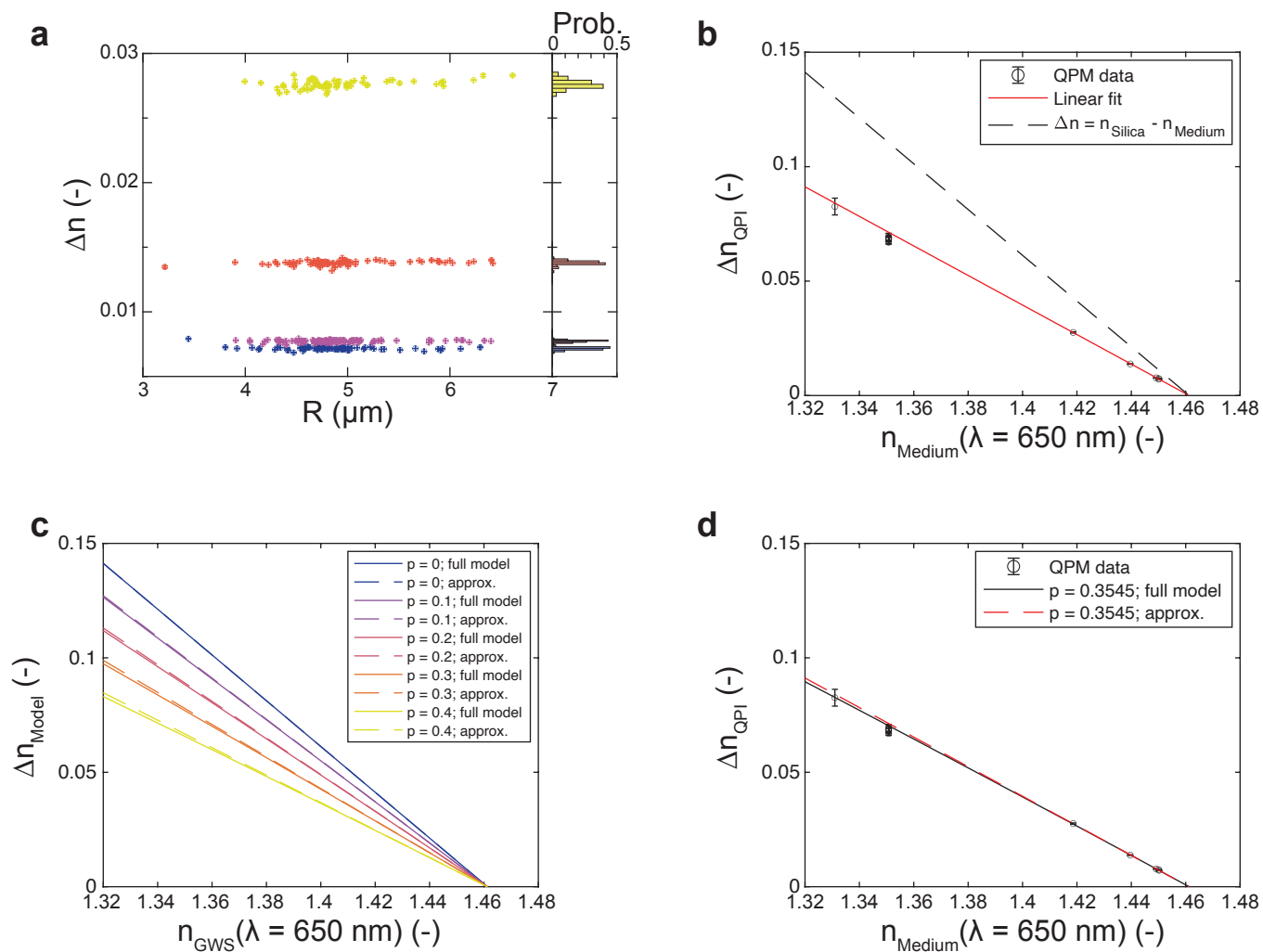
Extended Data Fig. 1: Estimate of capillary length for biomolecular condensates



691 **Extended Data Fig. 2: Silica bead measurements and porosity**

692 **a**, (left) Refractive index difference between silica beads and the surrounding glycerol/water
693 mixture as a function of bead size as measured by QPI for a range of glycerol/water ratios.
694 Glycerol weight fraction of the medium is 0.6641 (yellow, $N = 66$), 0.808 (orange, $N = 83$),
695 0.8688 (purple, $N = 102$), and 0.8751 (blue, $N = 74$). Datapoints represent individual beads,
696 error bars are 95% confidence intervals returned from fits, and are typically smaller than the
697 datapoint. Though the nominal bead diameter is 10 μm , the samples show significant
698 polydispersity. Importantly, there is no strong systematic variation of the extracted Δn with
699 bead size. (right) Measured refractive index distribution is approximately symmetric for each
700 condition. **b**, Population mean (\pm standard deviation) of Δn measured by QPI at $\lambda = 650$ nm
701 for silica beads as a function of the refractive index of the glycerol/water mixture, n_{medium} . Note
702 that n_{medium} was measured at $\lambda = 589$ nm on a digital refractometer and is plotted following
703 adjustment to $\lambda = 650$ nm using published dispersion relationships for glycerol and distilled
704 water and an approximate mixing rule, as described in Methods. Solid red line is a linear fit to
705 the data with the 4 largest x -values, with slope -0.6455 ± 0.01806 . The x -intercept of the fit
706 line, at which the refractive index of the silica bead is indistinguishable from that of the
707 medium, is 1.461 ± 0.057 . Importantly, this is comparable to published values of fused silica
708 under similar conditions (e.g. $n = 1.4565$ at 650 nm, 20 $^{\circ}\text{C}$, ⁶³), independently of whether we
709 adjust for dispersion. However, the slope of the fit line (-0.6455 ± 0.0181) differs significantly
710 from the value of -1 expected for beads of pure fused silica (dashed black line). This suggests
711 that the beads may be porous, as has been reported previously ⁶⁰. **c**, The refractive index
712 difference expected for silica beads with porosity p as a function of the refractive index of the
713 surrounding glycerol/water mixture, assuming that the bead pores are filled with the
714 glycerol/water mixture. Here p is the fraction of the bead volume occupied by pores rather than
715 silica. Different colors represent different values of porosity from 0 to 0.4. For each p , Δn is
716 calculated using two different refractive index mixing rules, either a weighted linear
717 combination (approx., dashed line) or the Lorentz-Lorenz relation (full model, solid line,
718 Methods). Both models predict that fluid-filled pores in the silica beads would give a Δn that
719 decreases (nearly) linearly with slope $(1-p)$ as n_{medium} increases. The two models are almost
720 indistinguishable except at low n_{medium} and high p , where the simple approximation noticeably
721 overestimates Δn . **d**, Same data as in **b** above, but now overlaid with model predictions for
722 silica beads with $p = 0.3545$. All measurements at 25 $^{\circ}\text{C}$.
723

Extended Data Fig. 2: Silica bead measurements and porosity

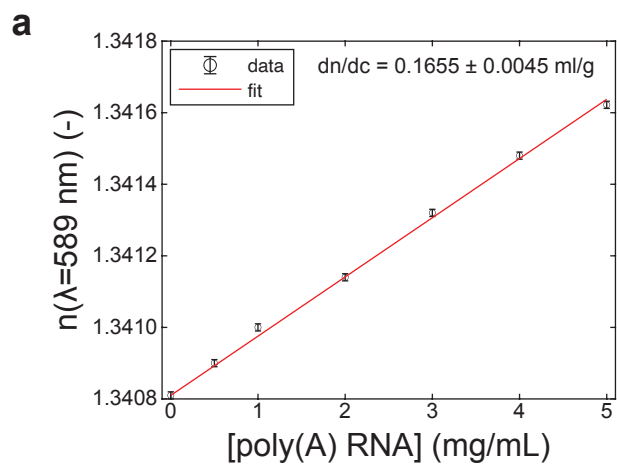


725 **Extended Data Fig. 3: Measurement of dn/dc for poly(A) RNA at 589 nm**

726 **a**, Refractive index of poly(A) RNA in water as a function of RNA concentration.
727 Measurements were performed with a digital refractometer at 589 nm at 20 °C. Error bars are
728 the larger of the standard deviation of $N = 5$ measurements or the instrument resolution 0.00001
729 (if all repeat measurements were identical). The refractive index increment is given by a linear
730 fit as 0.1655 ± 0.0045 ml/g.

731

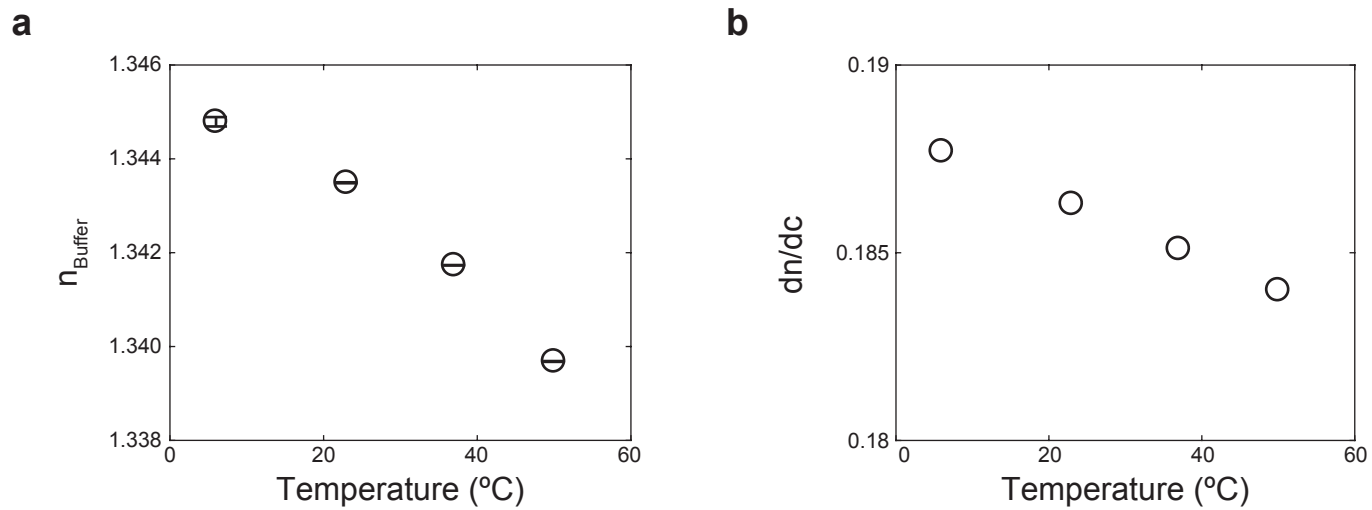
Extended Data Fig. 3: Measurement of dn/dc for polyA RNA at $\lambda = 589$ nm



733 **Extended Data Fig. 4: Temperature-dependent optical constants**

734 **a**, Refractive index of buffer as measured with a digital refractometer at 589 nm at the
735 temperatures used in Fig. 3f. Error bars are the larger of the standard deviation of $N = 5$
736 measurements or the instrument resolution 0.00001 (if all repeat measurements were identical).
737 The refractive index of the solution decreases with increasing temperature primarily due to the
738 reduced electron density accompanying thermal expansion. Note that the reduction in refractive
739 index due to this effect, $n_{buffer}(6\text{ }^{\circ}\text{C}) - n_{buffer}(50\text{ }^{\circ}\text{C}) = 0.0051$, is much smaller than the variation
740 of Δn we measure for TAF15(RBD) condensates over the same range, $\Delta n(6\text{ }^{\circ}\text{C}) - \Delta n(50\text{ }^{\circ}\text{C}) =$
741 0.0144. **b**, Refractive index increment for SNAP-TAF15(RBD) estimated using SEDFIT
742 software³² as a function of temperature. These values were used in Fig. 3f to convert the Δn
743 measured by QPI to the c_{cond} values reported at each temperature.
744

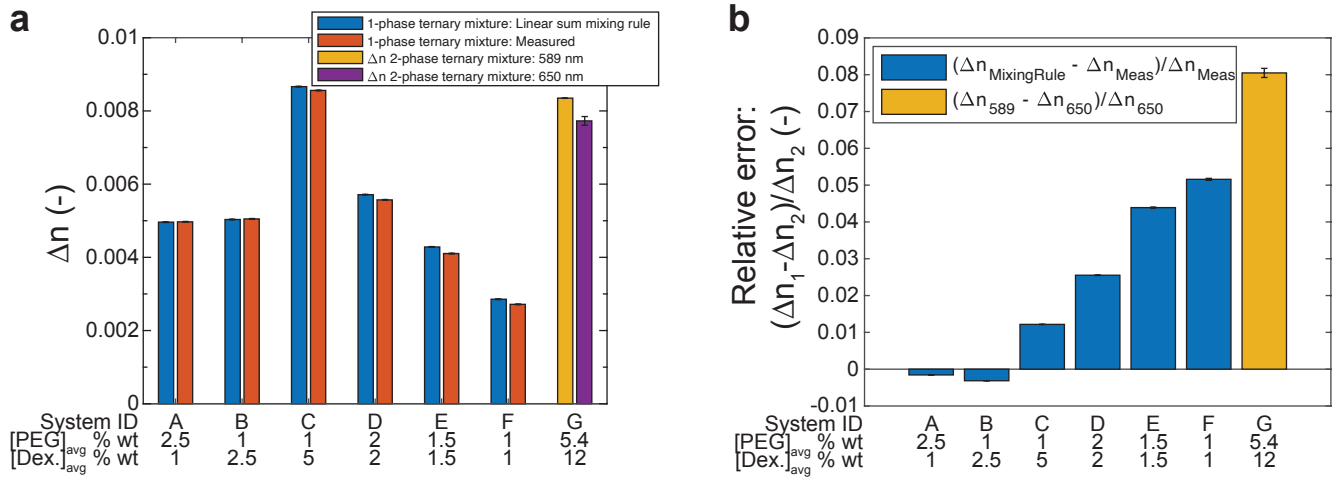
Extended Data Fig. 4: Temperature-dependent optical constants



746 **Extended Data Fig. 5: Validation of linear sum approximation for refractive index of**
747 **mixtures**

748 **a**, Refractive index difference between either homogeneous PEG/Dextran mixtures prepared
749 in the one-phase regime and water (blue and red) or between coexisting phases in the two-
750 phase regime (yellow and purple). Average system composition is specified below each bar as
751 weight fractions of PEG-35k and Dextran-500k. Blue bars show the refractive index measured
752 experimentally on a digital refractometer at 589 nm, while red bars show the refractive index
753 predicted for the same compositions using a linear sum approximation for the mixing rule (see
754 Methods). Yellow bar shows the difference between the refractive indices of the coexisting
755 phases, each measured individually at 589 nm on a digital refractometer. Purple bar shows the
756 population mean refractive index difference between the same phases measured via QPI for N
757 = 205 droplets. Error bars for digital refractometry measurements are the larger of the standard
758 deviation of $N = 5$ measurements or the instrument resolution 0.00001 (if all repeat
759 measurements were identical). Error bars for the predictions are estimated at 0.00001. Error
760 bar for the QPI measurement is the standard deviation of the measured Δn distribution. All
761 measurements were performed at 24 °C. **b**, Relative error of the paired measurements in **a**. The
762 relative error incurred by application of the linear sum mixing rule is typically much less than
763 5 %. For comparison, natural variation in optical properties with wavelength (dispersion)
764 results in an 8% change in Δn between 589 nm and 650 nm.
765

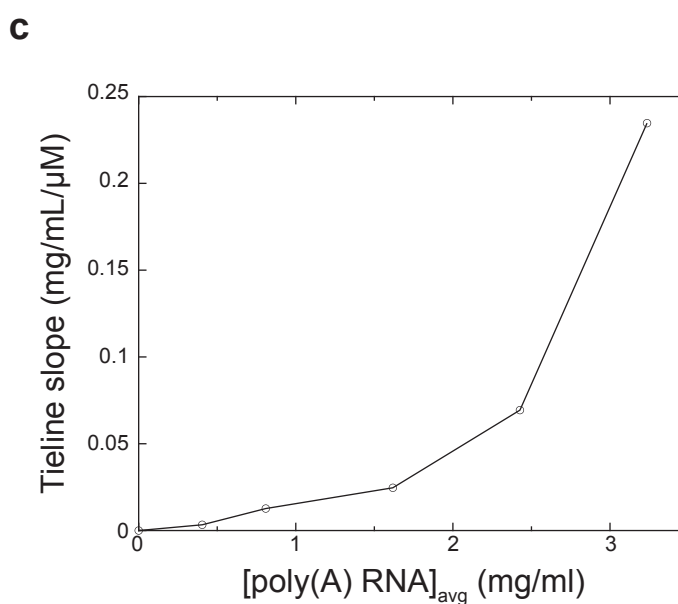
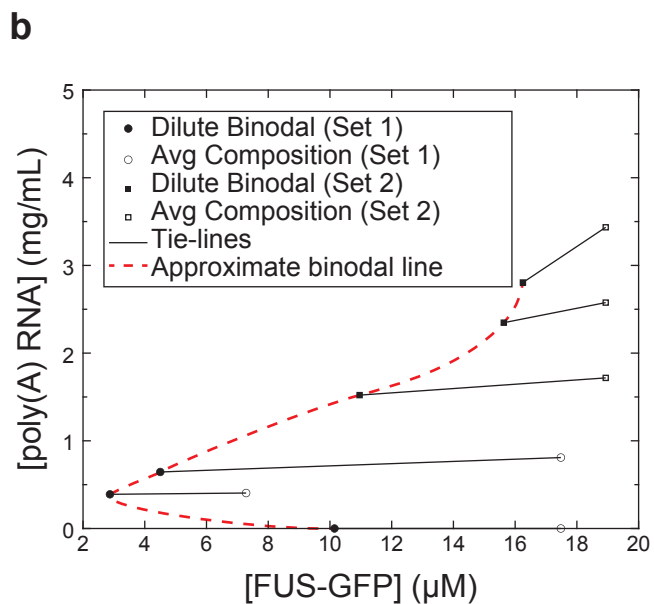
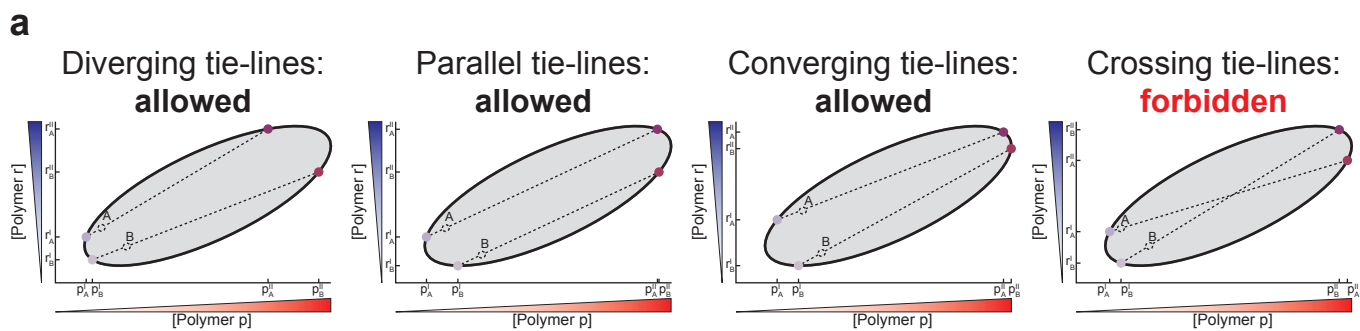
Extended Data Fig. 5: Validation of linear sum approximation for refractive index of mixtures



767 **Extended Data Fig. 6: Examples of physically permissible tie-lines**

768 **a**, Examples of ternary phase diagrams with varying tie-line orientations. While tie-lines can
769 in principle diverge (left), be parallel (center-left), or converge (center-right), it is unphysical
770 and thus forbidden for them to cross within the multi-phase coexistence region (right). **b**,
771 Ternary phase diagram for FUS/poly(A) RNA on linear scales zoomed in on the dilute
772 binodal. **c**, Slopes of the tie-lines shown in **b**. Relative to the classification scheme introduced
773 in **a**, this system displays diverging tie-lines.
774

Extended Data Fig. 6: Examples of physically permissible tie-lines

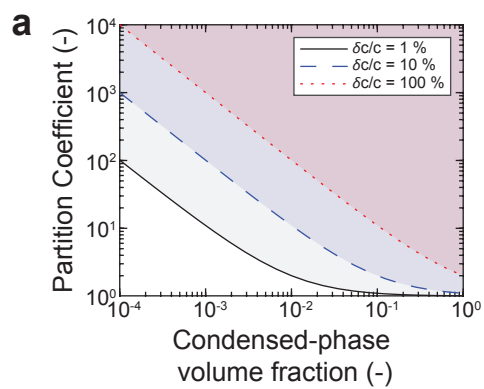


776 **Extended Data Fig. 7: Multi-component detection limits**

777 **a**, The minimum partition coefficient P_{min} for which the concentration of a species in the dilute
778 phase c^I is measurably different from its total average concentration in the system \bar{c} depends
779 on the relative precision $\delta c/c$ of the dilute-phase detection strategy. For a given $\delta c/c$, P_{min}
780 decreases as the volume fraction of the condensed phase increases. In this diagram, curves
781 show the minimum partition coefficient for which partitioning of an arbitrary species would be
782 detectable in a system as a function of condensed-phase volume fraction for $\delta c/c = 1\%$ (solid
783 black), 10% (blue dashed), and 100 % (red dotted). The shading denotes that all partition
784 coefficients above the corresponding lower-limit are detectable.

785

Extended Data Fig. 7: Multi-component detection limits



787 **Supplementary Video 1**
788 Quantitative phase imaging of aging timecourse for reconstituted PGL3 condensates.
789

790

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